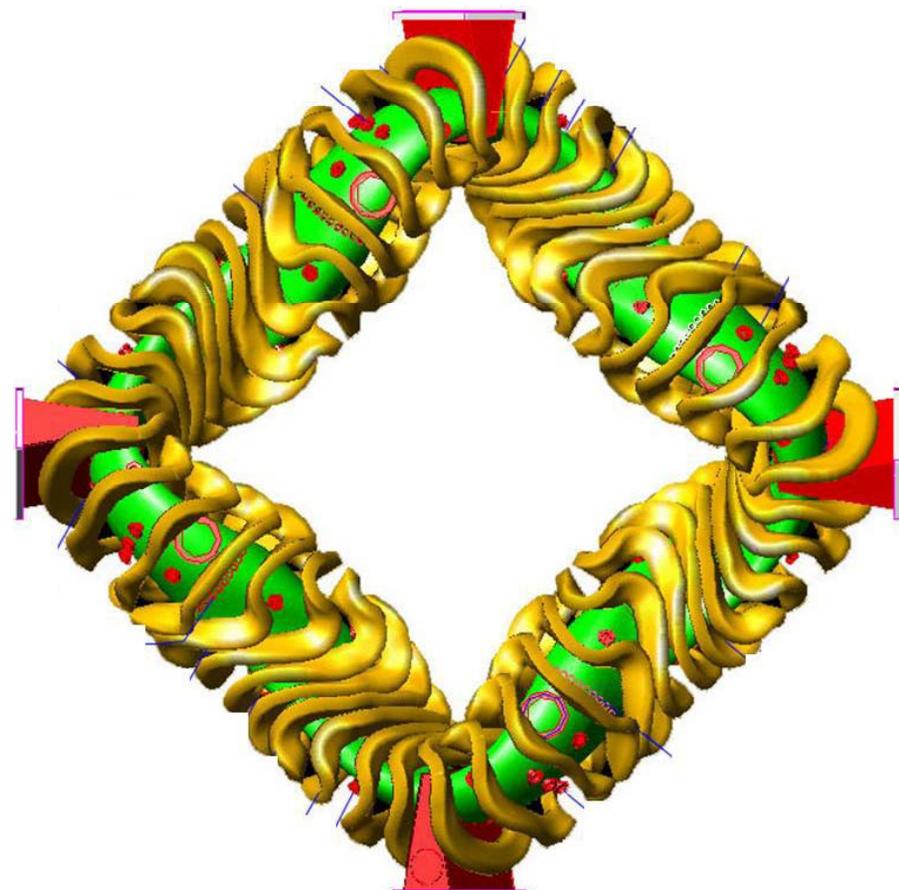
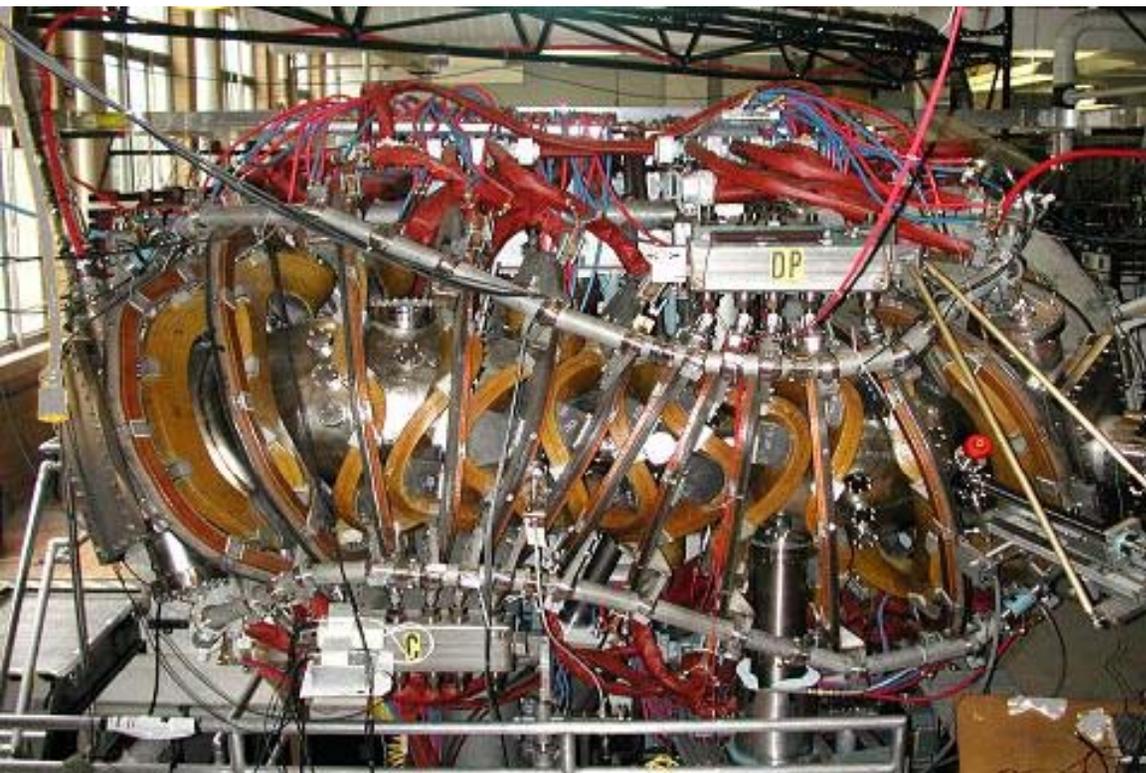


Neoclassically Driven Electron Transport Barrier in the HSX Stellarator



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10/12/2009

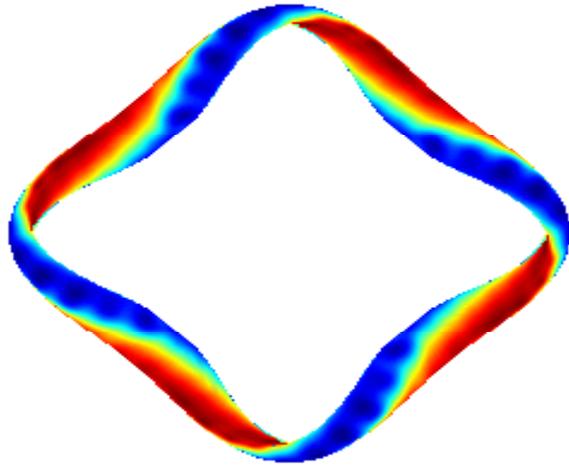
Special thanks to: Walter Guttenfelder (U. Warwick), Don Spong (ORNL), HSX Team



Outline

- Description of the HSX stellarator
- Evidence of electron transport barrier driven by neoclassical E_r profile
 - Peaked T_e profiles measured, electron root E_r with strong radial shear predicted
- 2D turbulent transport model used to describe anomalous transport
 - Peaked T_e profiles only reproduced when ExB shear included
- Density threshold for achieving transport barrier observed for fixed input power
 - Consistent with neoclassical ion root predictions
- Large parallel flow measured and predicted (10-25 km/s)
 - This flow and associated fluxes are accounted for in momentum conserving NC analysis (PENTA)

HSX is Quasi-Helically Symmetric

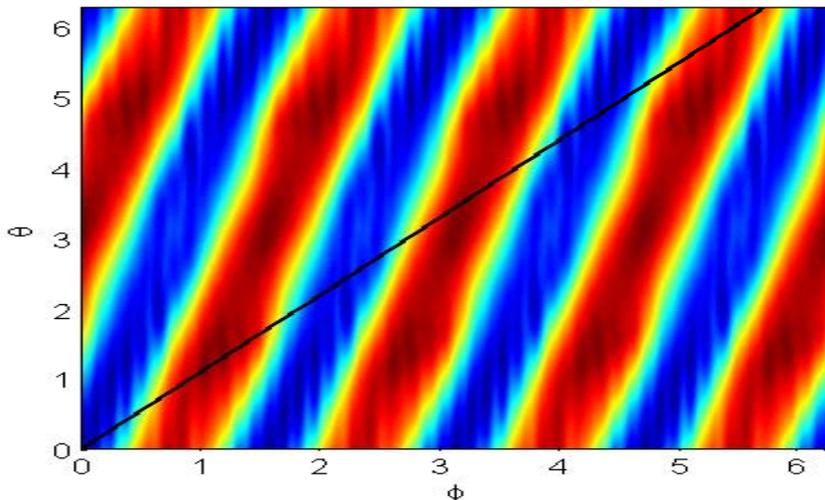


- QHS: helical direction of symmetry in $|B|$
- Effective transform is larger than physical transform
- Symmetry breaking $< 1\%$ at edge

Tokamak: $B / B_0 \cong 1 - \varepsilon_t \cos t\phi$

QHS: $B / B_0 \cong 1 - \varepsilon_h \cos(n - m\iota)\phi$

$\underbrace{\hspace{10em}}_{\iota_{\text{eff}} \sim 3}$

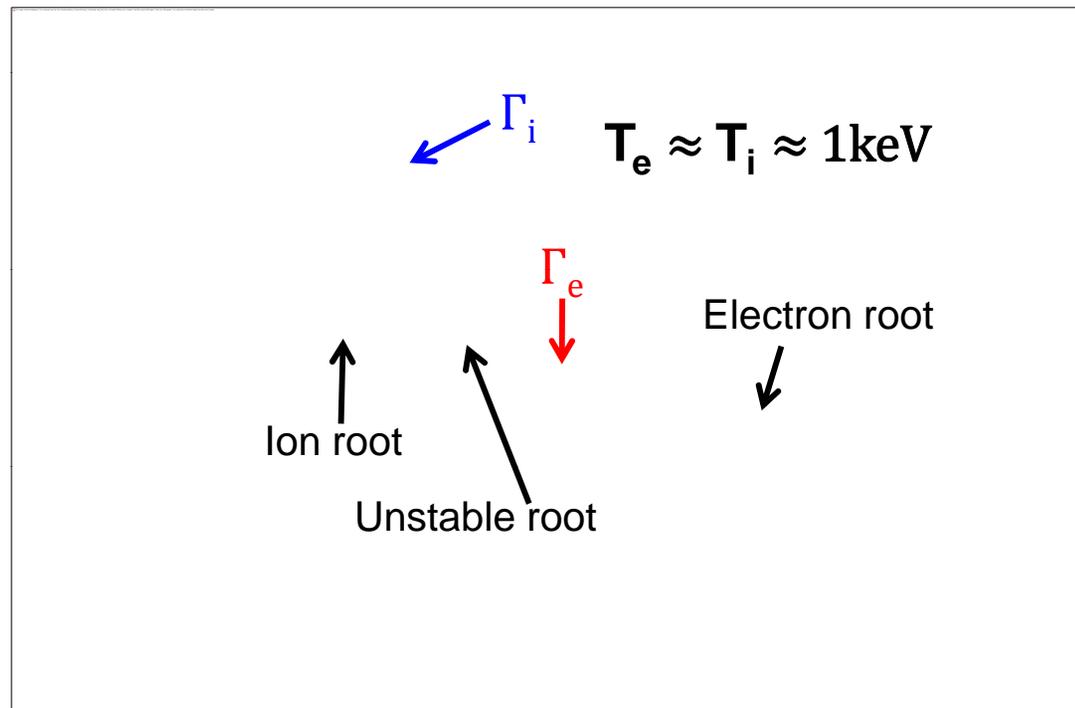


HSX Parameters

$\langle R \rangle$	1.2 m
$\langle a \rangle$	0.12 m
ι	1.05 \rightarrow 1.12
B_0	0.5 -1.0 T
ECRH 28 GHz	<100 kW

Calculating the Radial Electric Field

- E_r is determined by enforcing ambipolarity
- LMFP with $T_e \approx T_i$ results in three roots

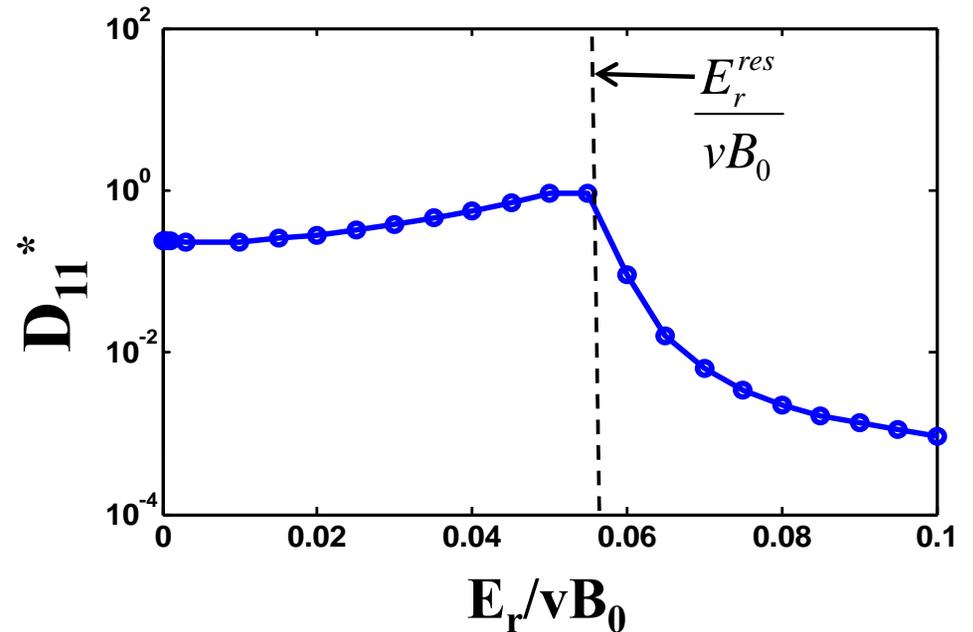
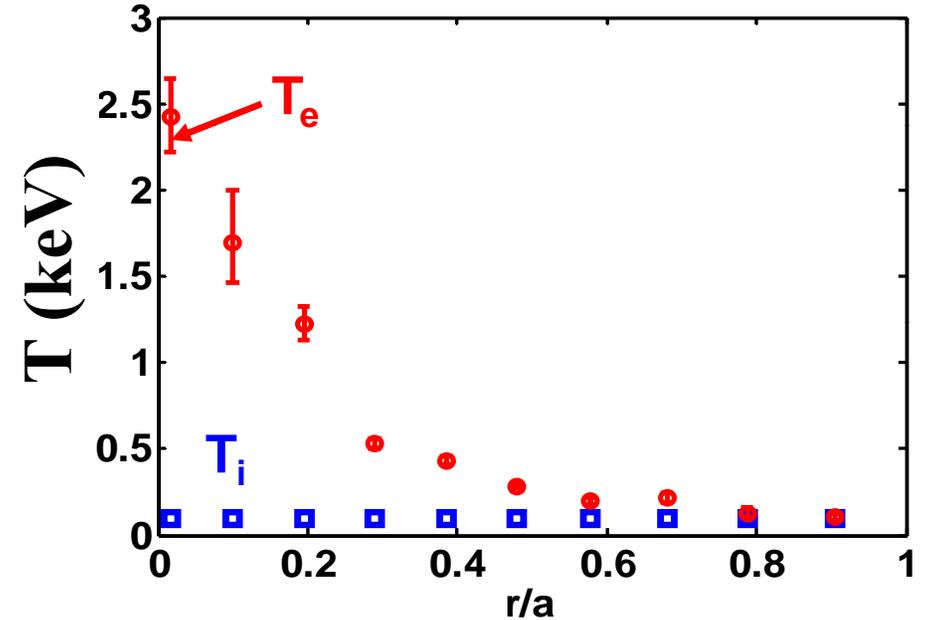


- Electron root can be reached by increasing Γ_e
- When $T_e \gg T_i$ the ion root solution may not exist near the core

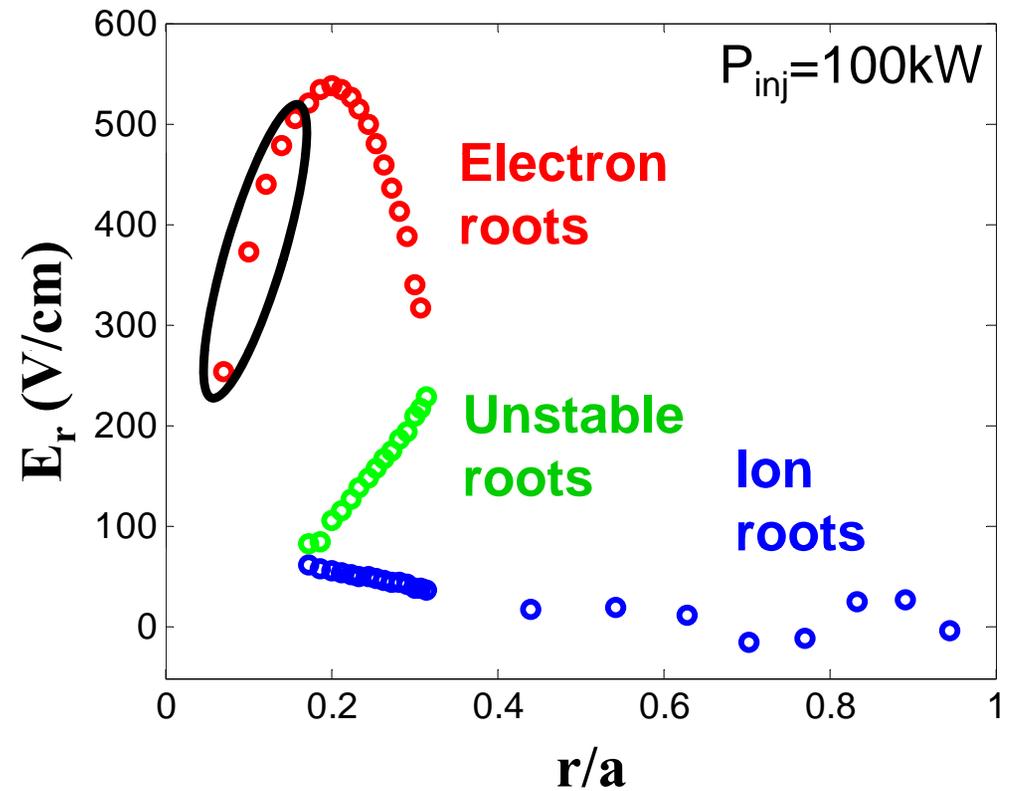
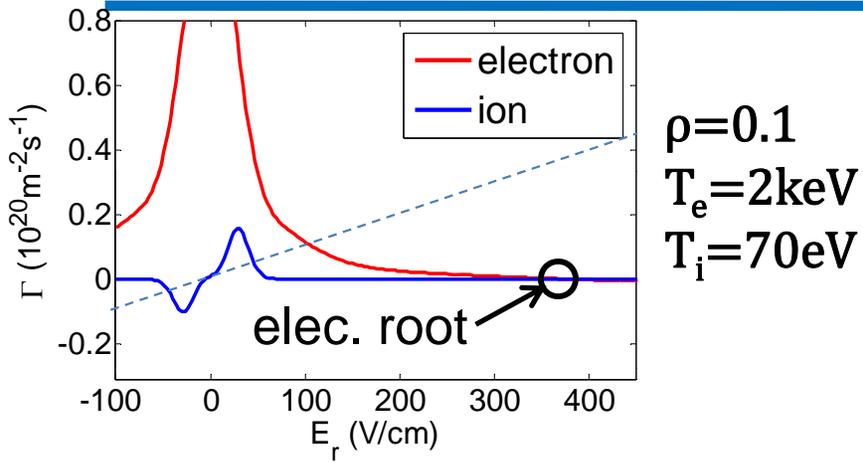
HSX Can Achieve Electron Root Because

$$T_e \gg T_i$$

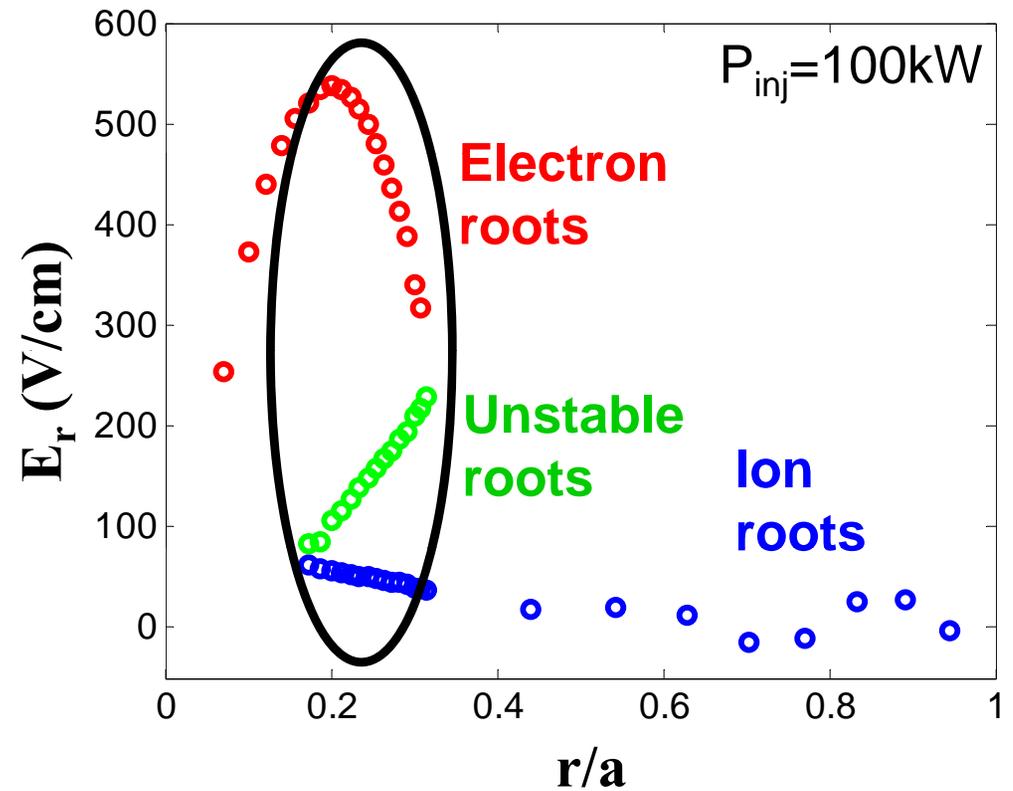
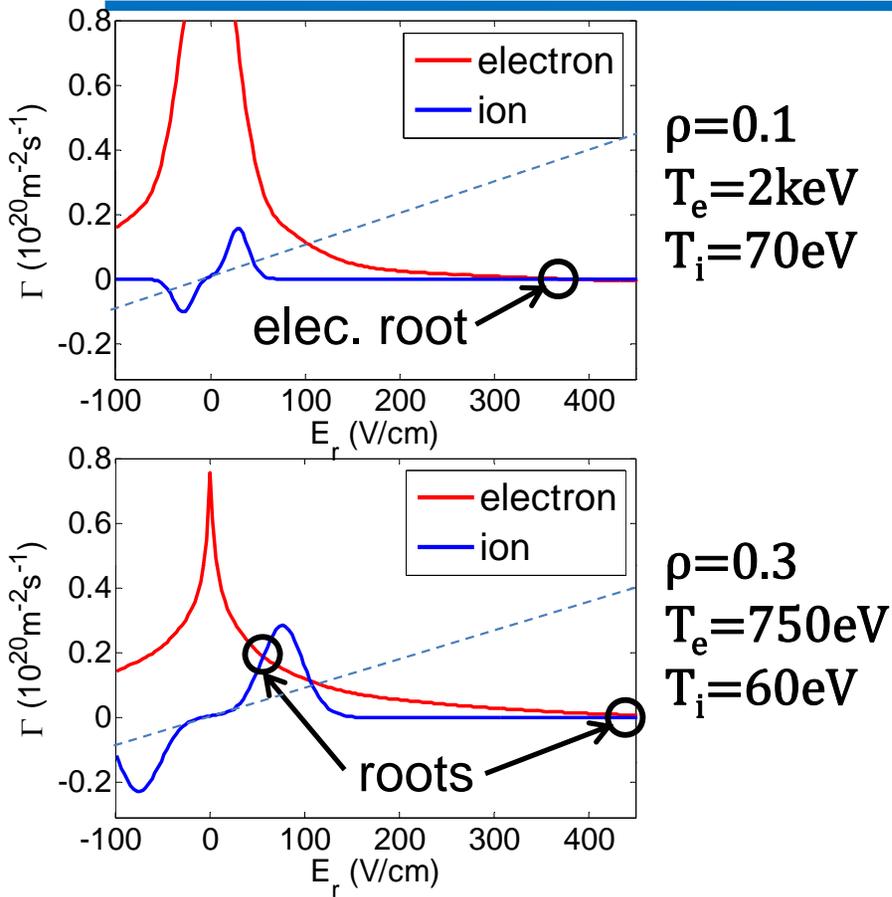
- In HSX $T_e \gg T_i$ over most of the plasma radius, with a strongly peaked T_e profile
- For $T_i \approx 100\text{eV}$, ions experience a resonance at modest E_r near plasma core
- The resonance occurs when poloidal velocity is canceled by the poloidal $\mathbf{E} \times \mathbf{B}$ drift
- Radial transport is increased near the resonance, and is strongly reduced for $E_r > E_r^{\text{res}}$



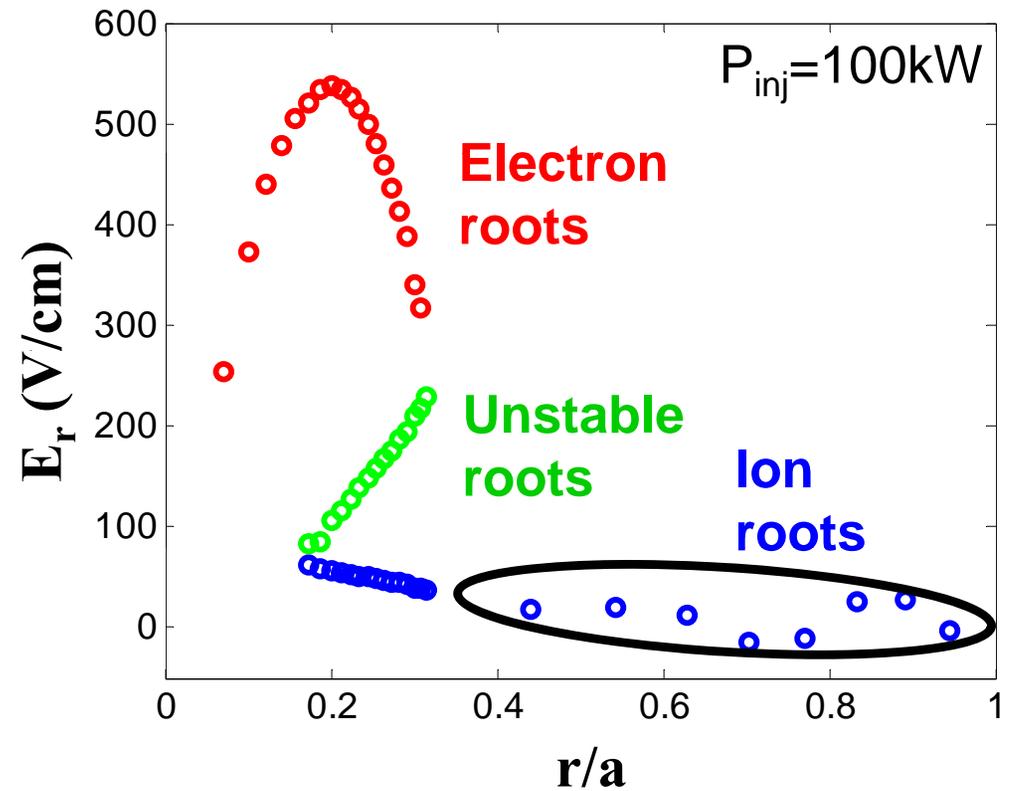
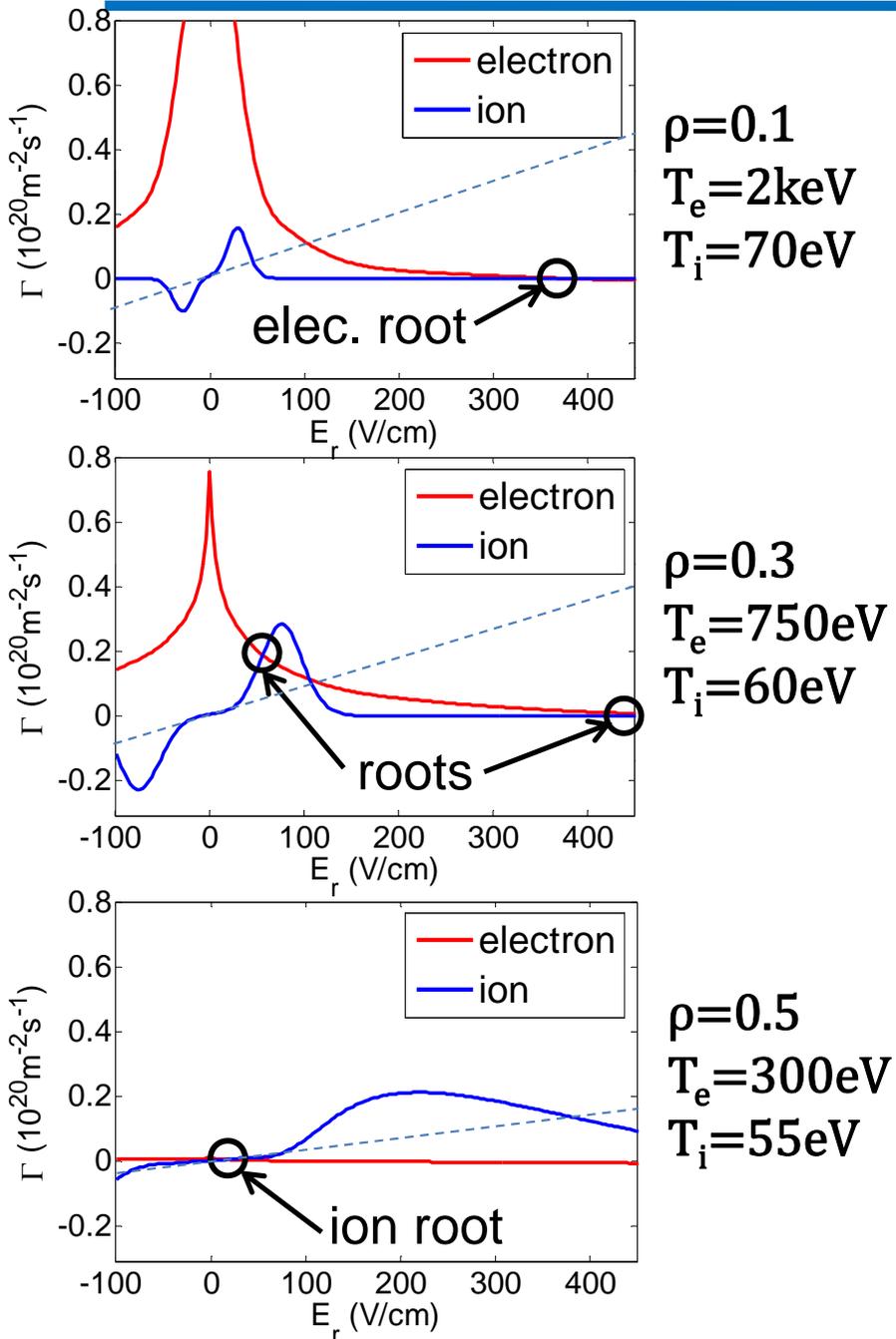
Radial Electric Field Roots in HSX



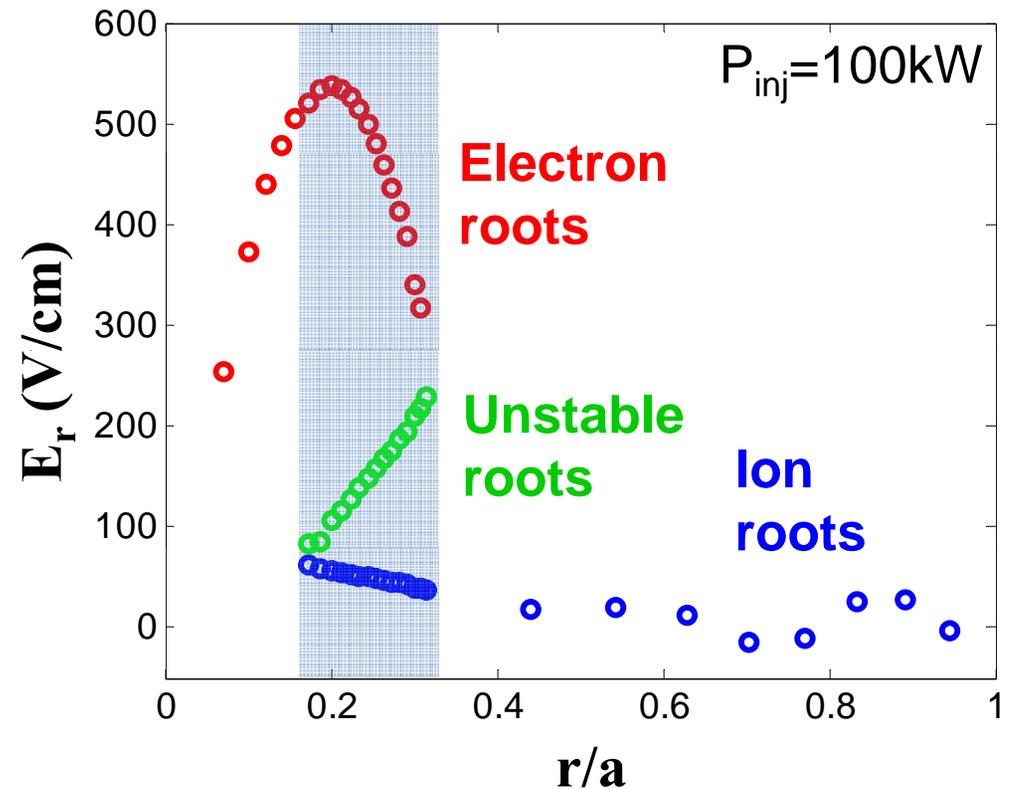
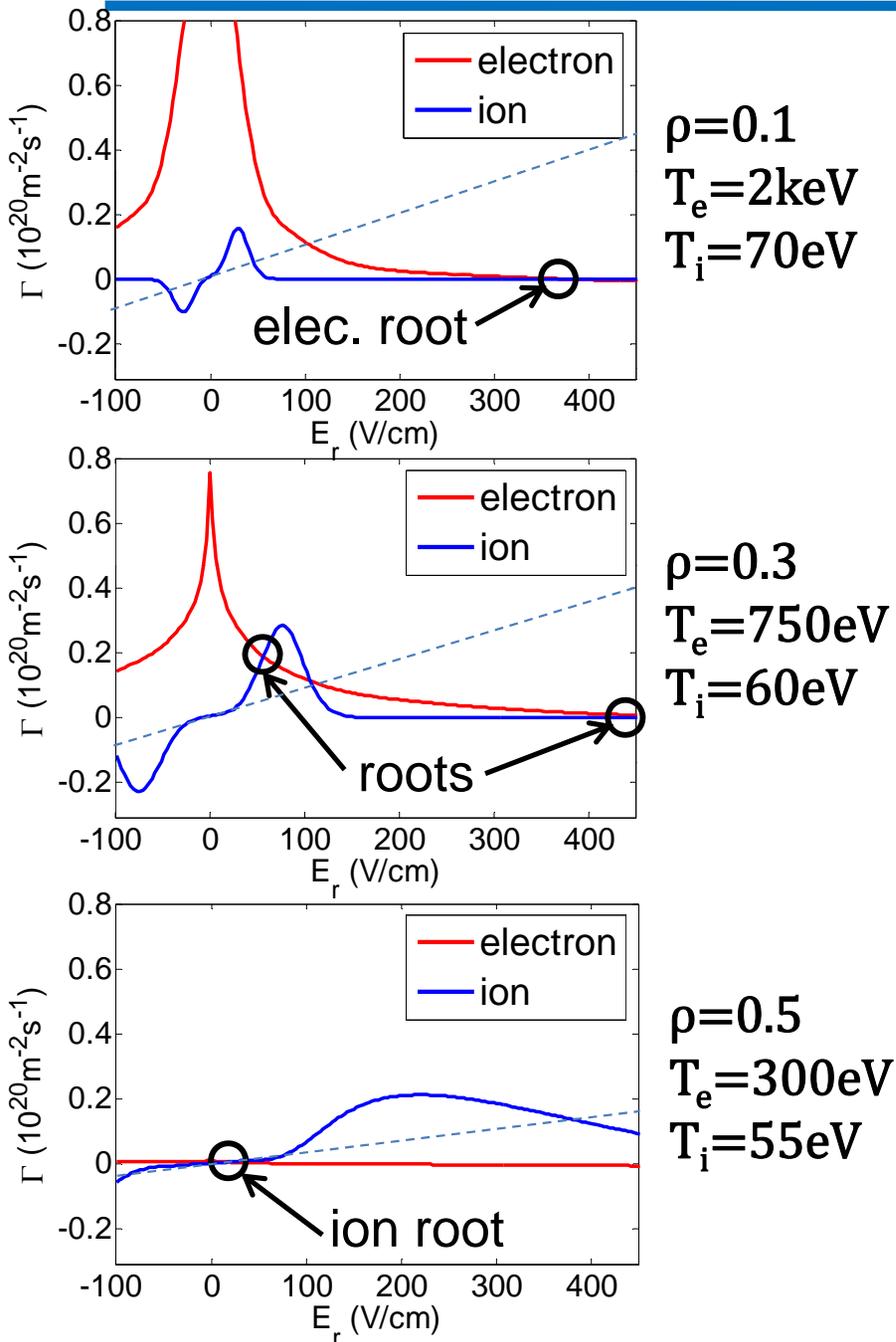
Radial Electric Field Roots in HSX



Radial Electric Field Roots in HSX



Radial Electric Field Roots in HSX

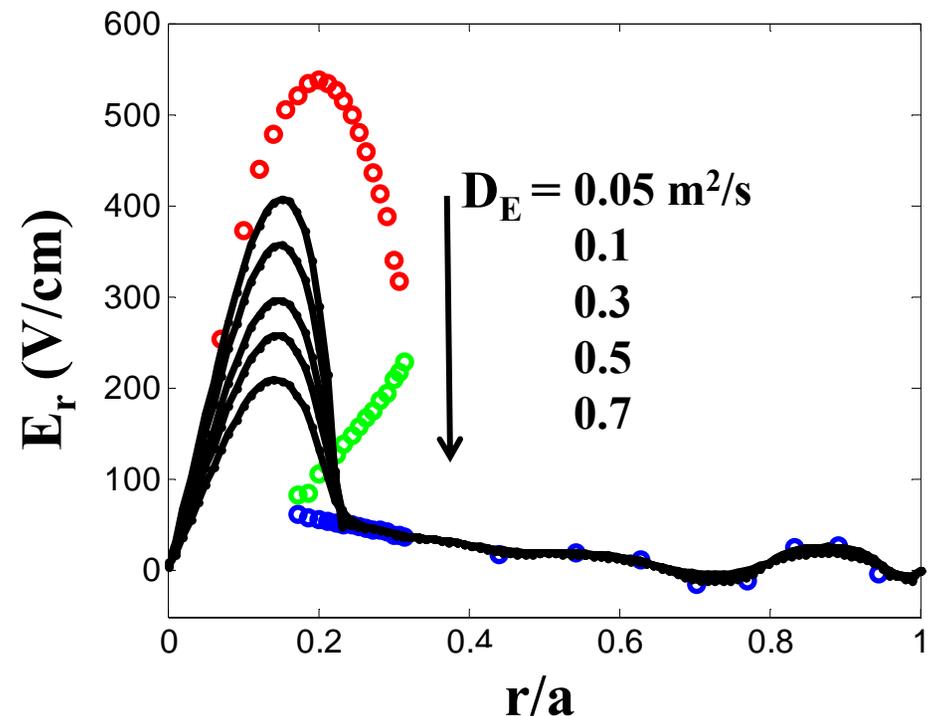


- **Only electron root in core, and only ion root towards edge**
 - Somewhere in three root region there is a transition, with strong E_r shear
 - Determining shear layer involves perpendicular viscosity

Solving the Diffusion Equation for E_r

- The radial electric field profile can be determined by solving a diffusion equation¹
- D_E (related to perpendicular viscosity) is generally not known
 - Solutions for different D_E show a region of strong E_r shear at $r/a \sim 0.25$

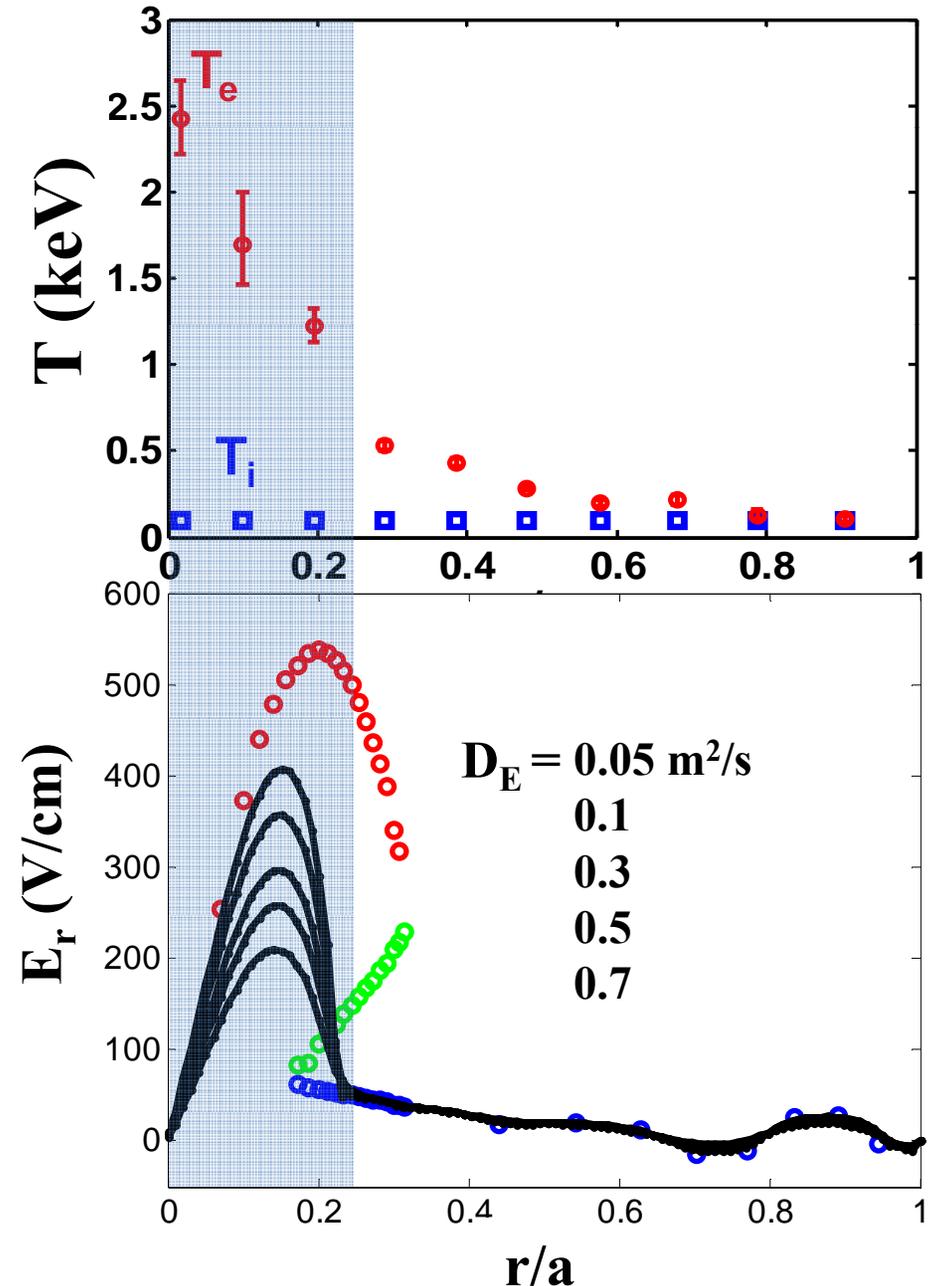
$$\frac{\partial E_r}{\partial t} - \frac{\partial}{\partial V} \left[\langle \nabla V \rangle D_E \left(\frac{\partial E_r}{\partial r} - \frac{E_r}{r} \right) \right] = \frac{e}{\epsilon_{\perp}} (\Gamma_e - \Gamma_i)$$



1) Shaing and Callen (1983), Maassberg *et al* (1993).

Strong E_r Shear is Predicted in Region of Peaked T_e

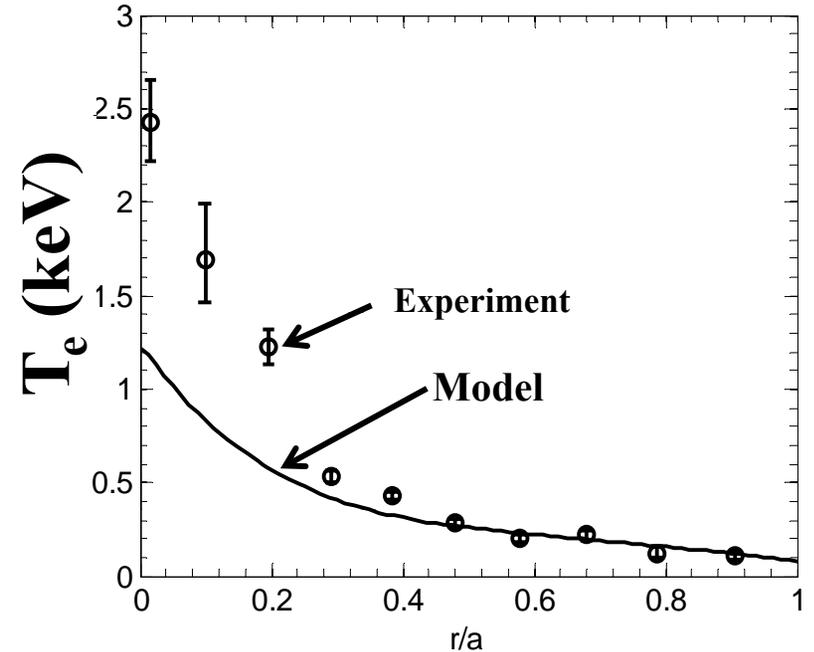
- The radial electric field profile can be determined by solving a diffusion equation¹
- D_E (related to perpendicular viscosity) is generally not known
 - Solutions for different D_E show a region of strong E_r shear at $r/a \sim 0.25$
- T_e peaking occurs within the strong E_r shear region
 - E_r shear can suppress turbulent transport



1) Shaing and Callen (1983), Maassberg *et al* (1993).

Applying a 2D Turbulent Transport Model to QHS

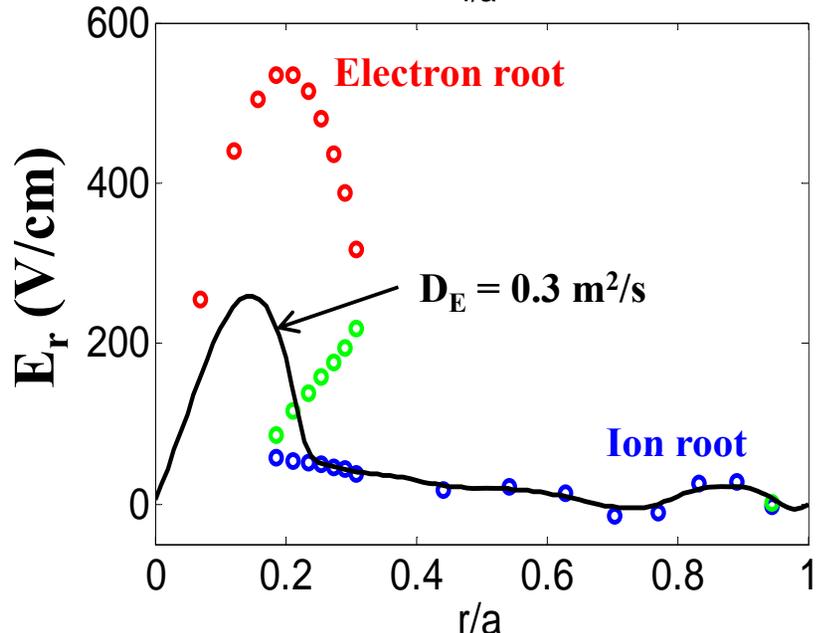
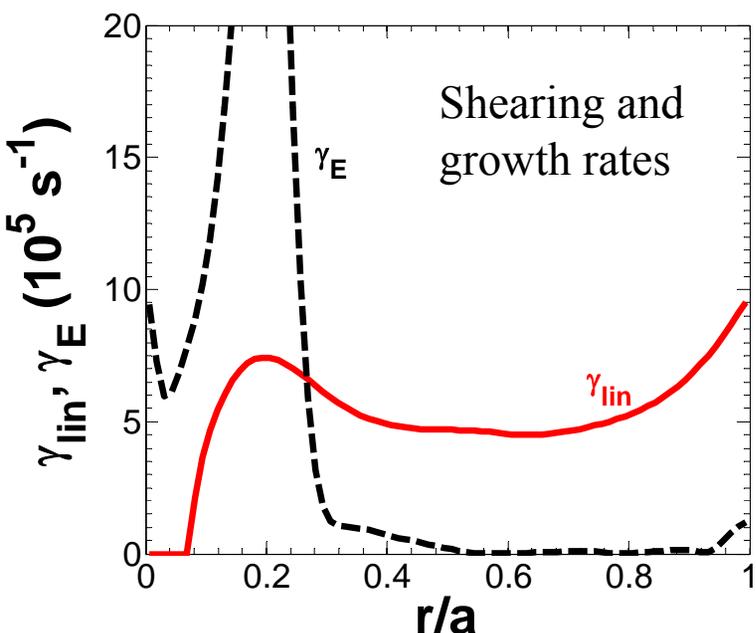
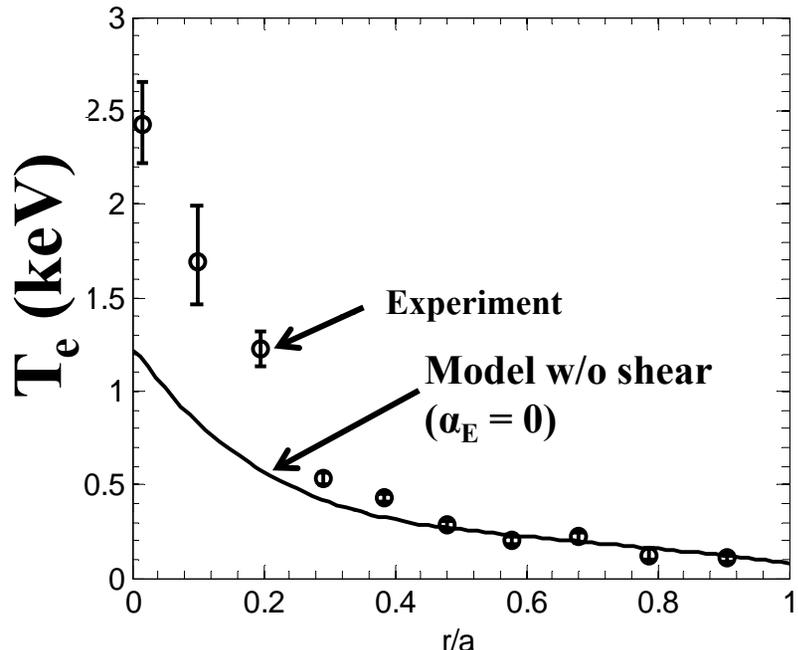
- The 2D quasi-linear Weiland model has been used to model turbulent transport in QHS
 - Like a tokamak, QHS has a single class of trapped particles.
 - With local geometry considerations, good agreement with 3D gyrokinetic GS2 growth rates.
 - Stored energy and confinement times predicted within 10%
- Predictive transport (NC + Turb.) simulations underestimate T_e in core
 - Turbulent diffusivity in this region is 10x experimental
 - Transport can be reduced via ExB shear



ExB Shearing Rate \gg Linear Growth Rate for $r/a < 0.3$

- ExB shear suppression is modeled using a linear quench rule:¹

$$D \Rightarrow D \cdot \max \left(1 - \alpha_E \frac{\gamma_E}{\gamma_{\max}}, 0 \right)$$
 - γ_E = ExB shear rate
 - γ_{\max} = maximum linear growth rate
- Shear suppression expected inside of $r/a = 0.3$

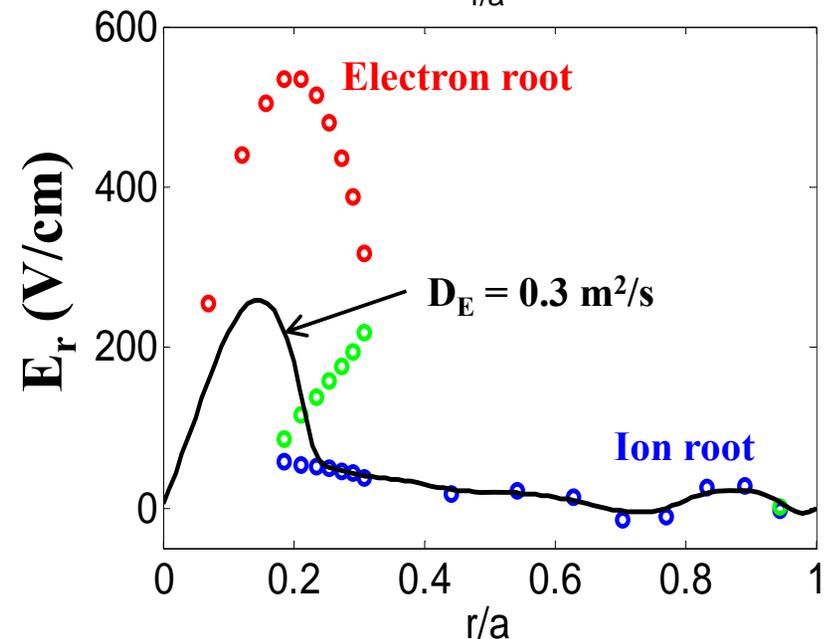
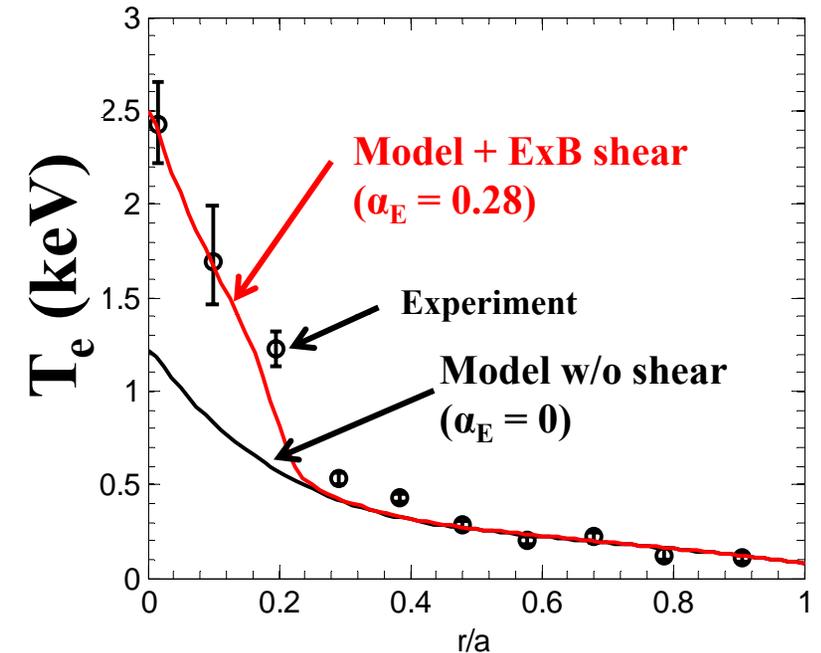
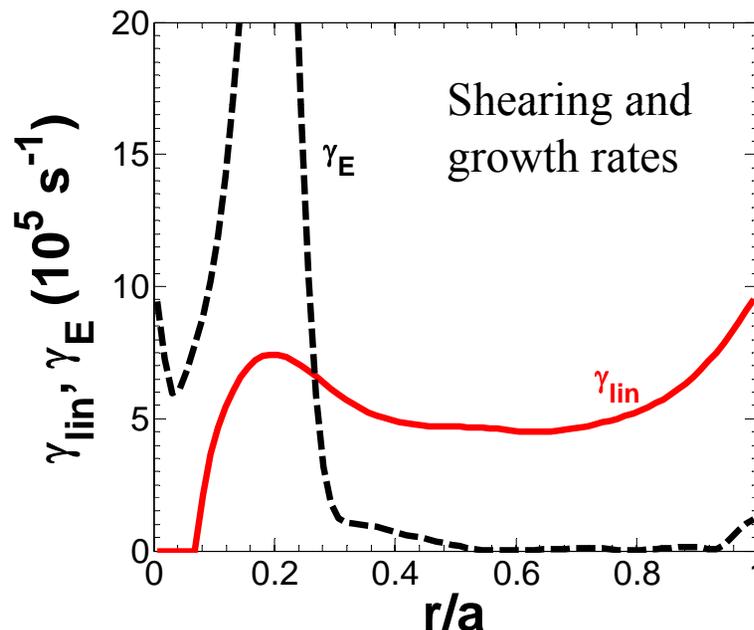


Guttenfelder, Lore, *et. al.*, (2008), 1) Kinsey (2005)

Turbulence Suppression via ExB Shear can Reproduce Experimental Profiles

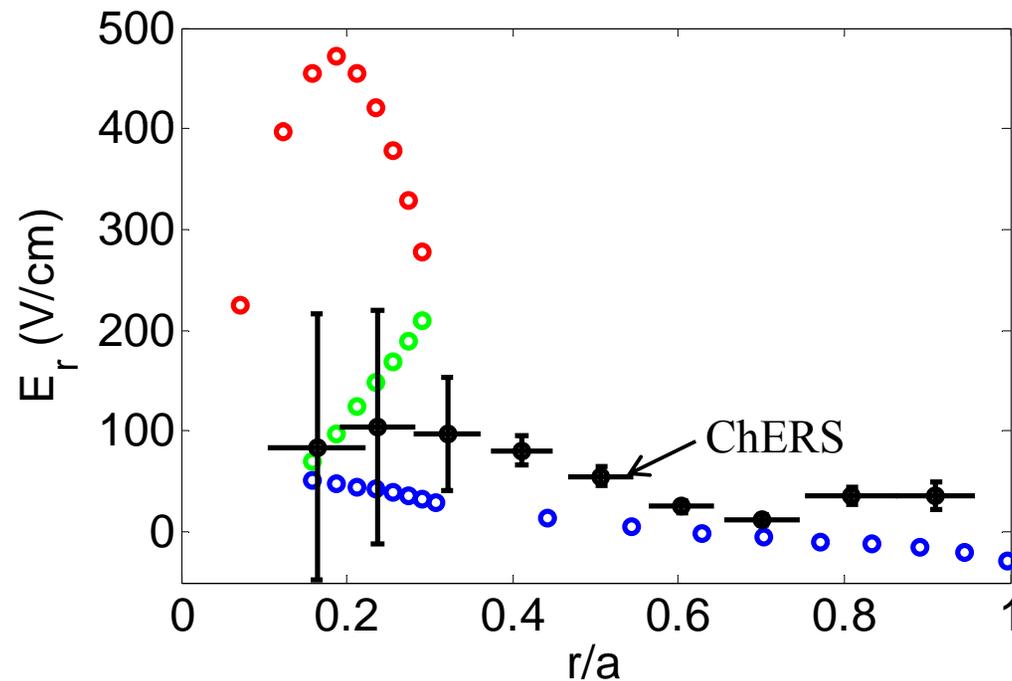
- ExB shear suppression is modeled using a quench rule:¹

$$D \Rightarrow D \cdot \max \left(1 - \alpha_E \frac{\gamma_E}{\gamma_{\max}}, 0 \right)$$
 - γ_E = ExB shear rate
 - γ_{\max} = maximum linear growth rate
- E_r shear required to reproduce peaking of experimental T_e profile
- Coupled turbulent and NC transport model can self-consistently explain measured T_e profiles**



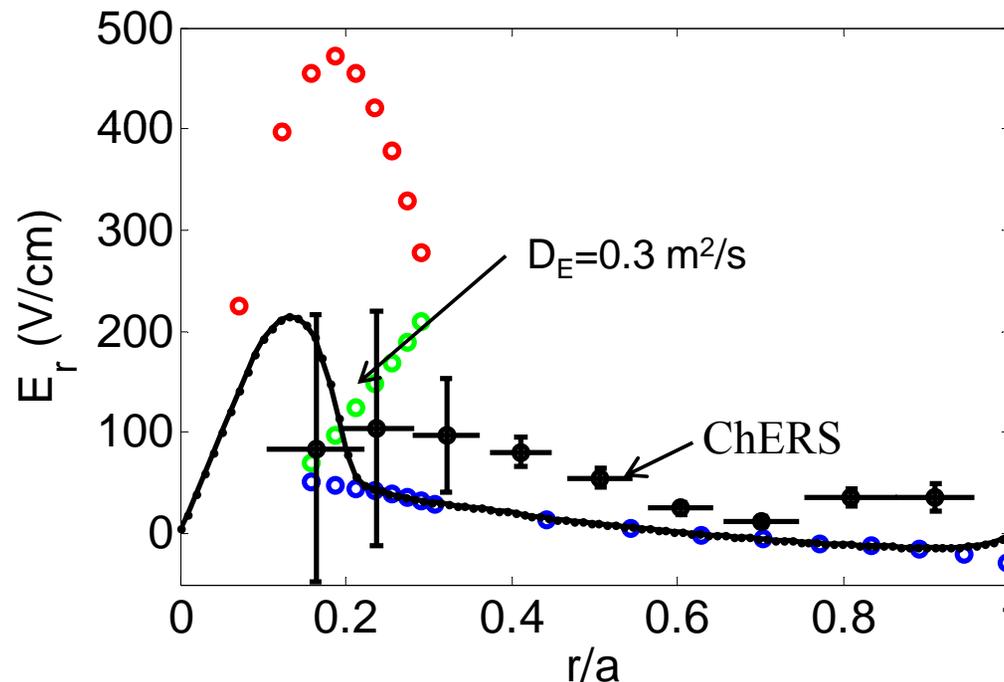
ChERS Measurements are Inconclusive in Plasma Core

- No measurements exist in region of electron root only solutions
- Large uncertainties due to beam width, flux surface shaping
- Edge measurements are consistent or larger than ion root



Most of Shear Region is Inside of Measurements

- No measurements exist in region of electron root only solutions
- Large uncertainties due to beam width, flux surface shaping
- Edge measurements are consistent with or larger than ion root solutions
- Only central measurement is within shear region, smoothing may occur here due to radial extent of measurements
- See Briesemeister poster this afternoon (P01-04)



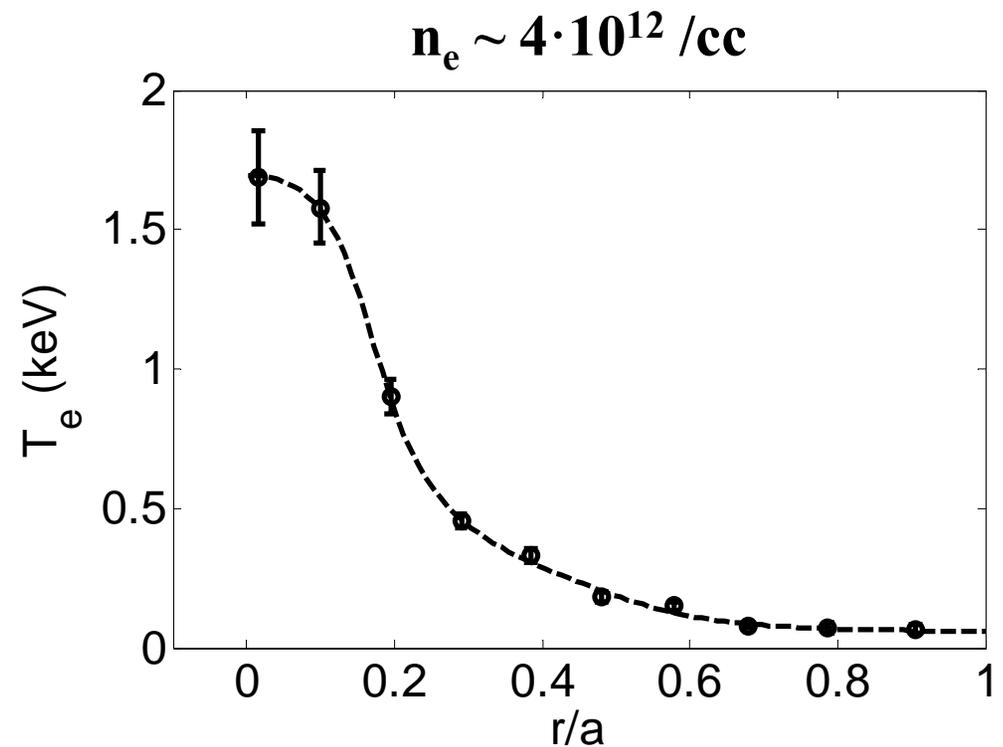
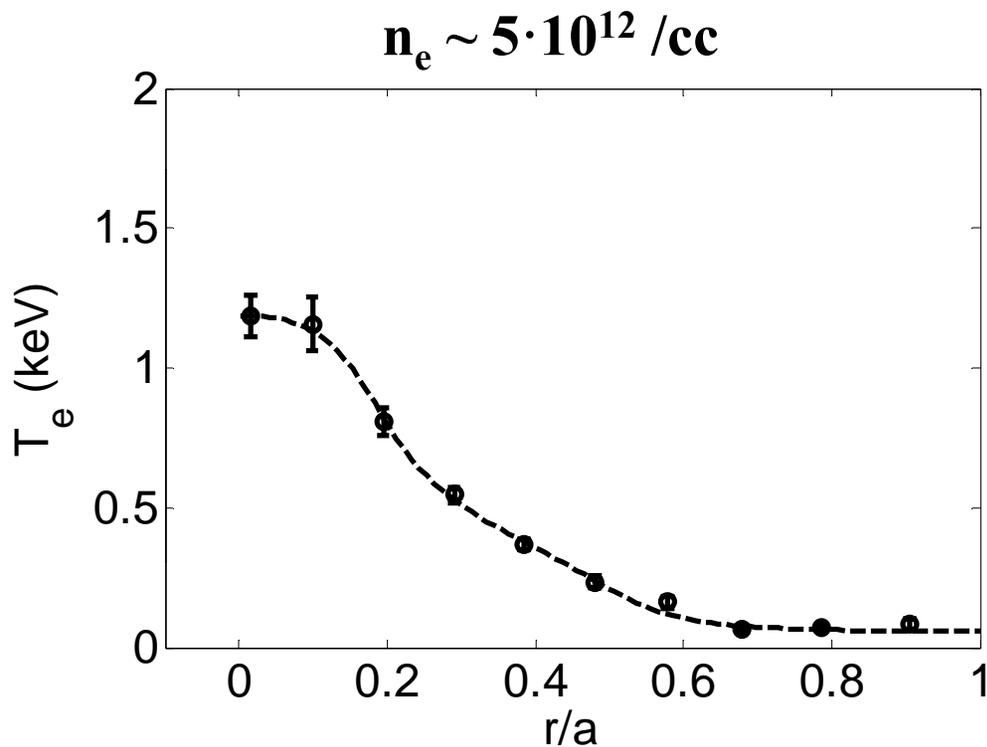
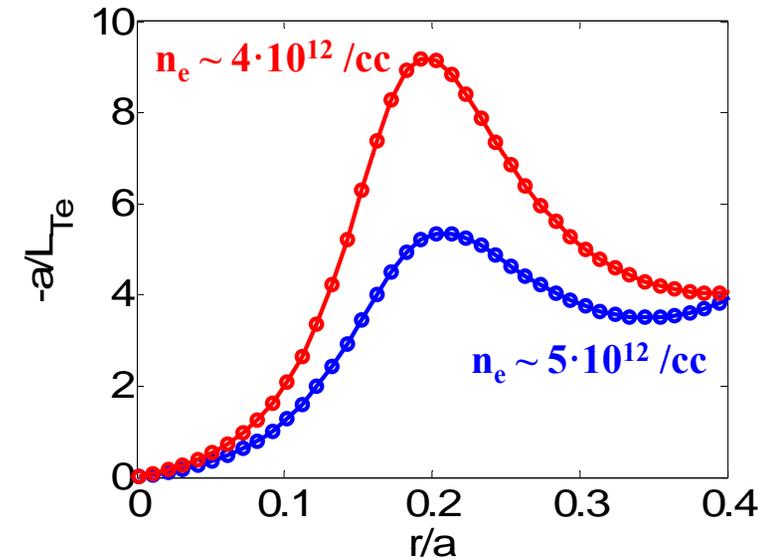
CERC Transport Barriers

- CERC (Core Electron Root Confinement) transport barriers have been observed in several other stellarators¹
 - Characterized by peaked T_e profiles, neoclassical electron root E_r
- One common feature is the existence of thresholds for achieving a CERC in P_{inj} and density
 - Thresholds often attributed to ECRH effects (conv. fluxes)
- Recent experiments indicate a threshold in QHS plasmas

1) Yokoyama, *et. al* (2006, 2007)

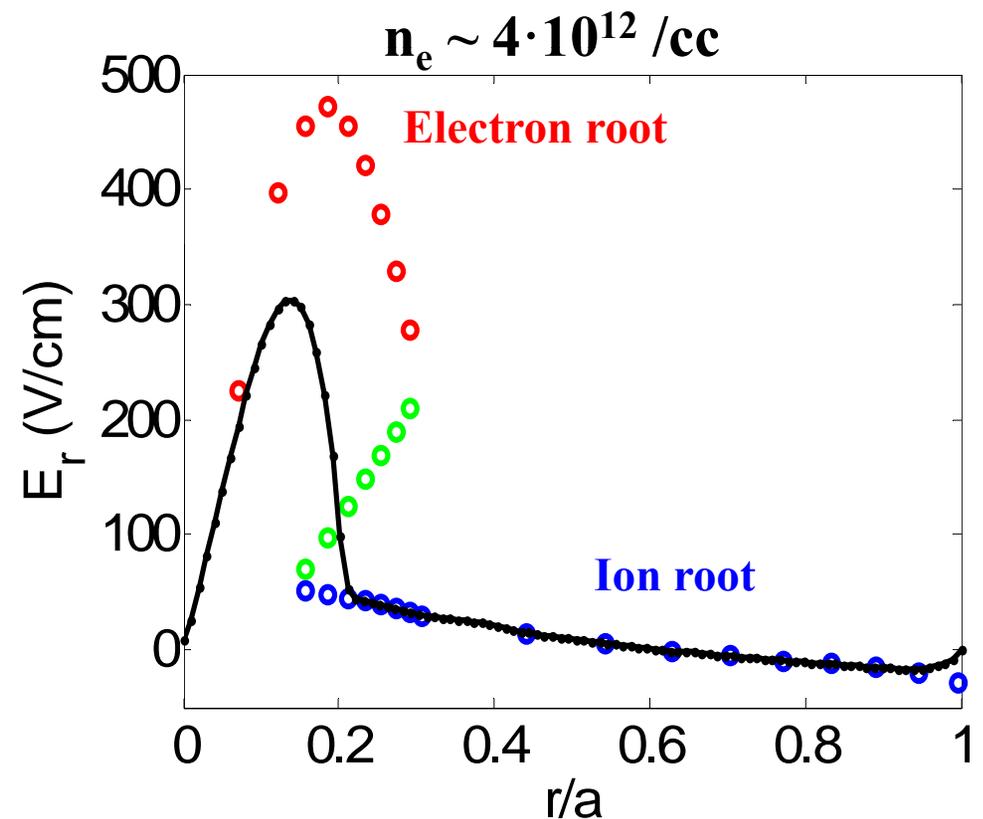
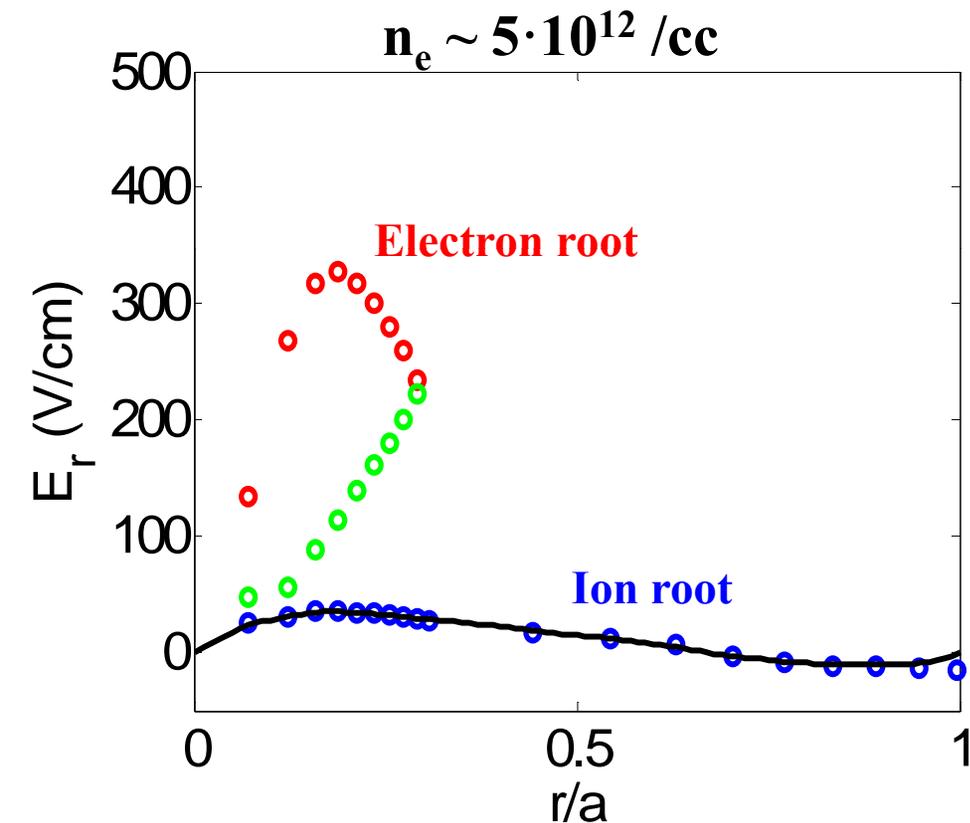
Recent Experiments Suggest a CERC Density Threshold

- For same input power, higher density results in less peaked T_e profile
 - $P_{inj} = 50\text{kW}$
- At higher density a/L_{Te} is 2x smaller in core



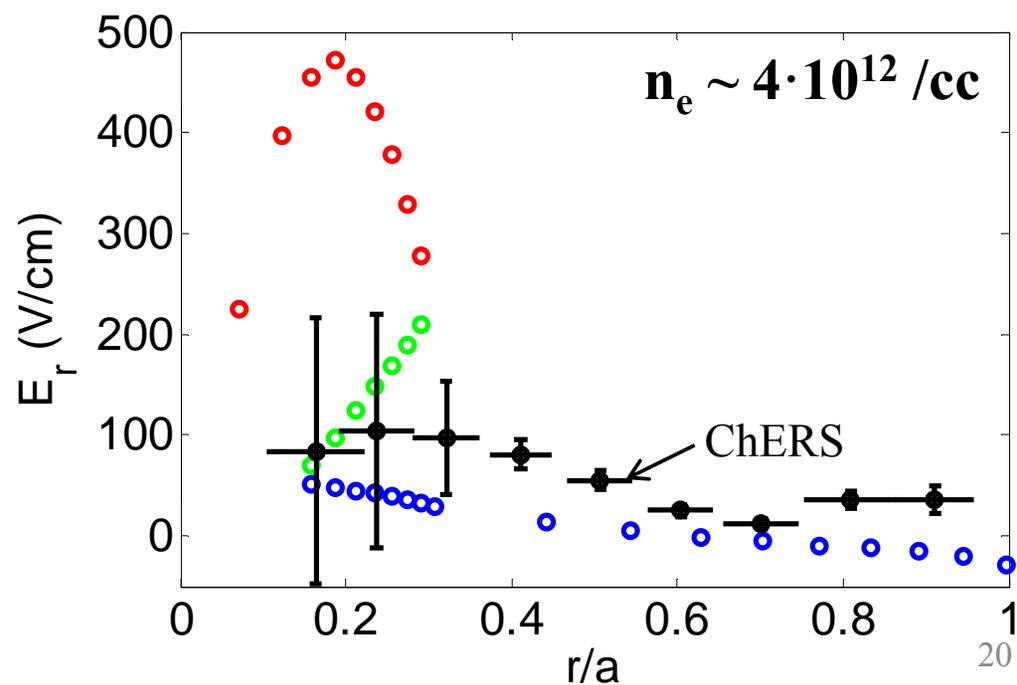
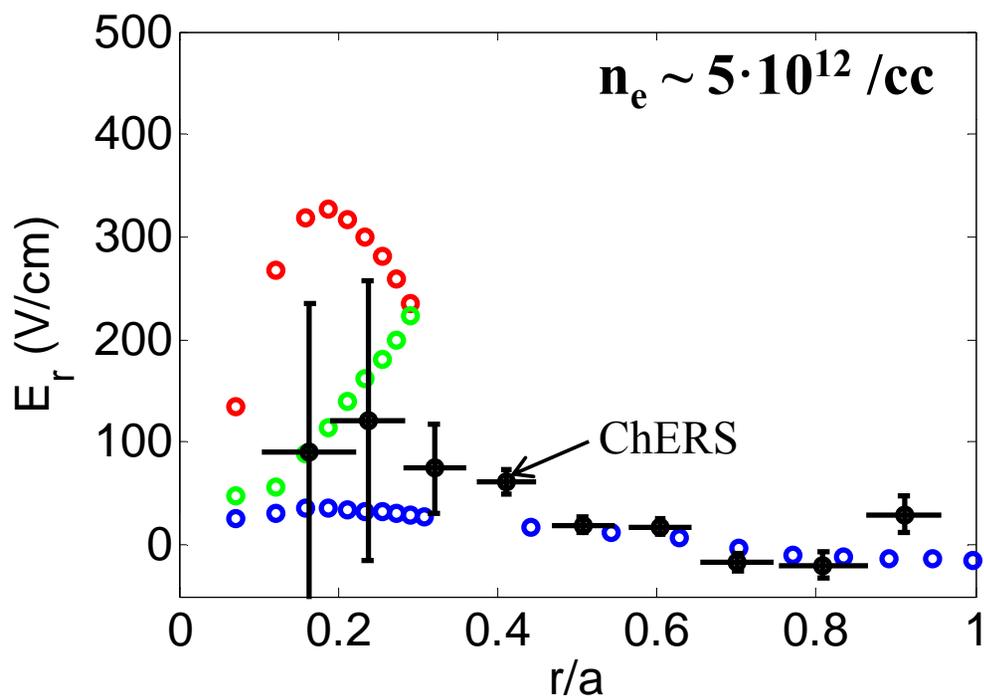
Ion Root is Predicted Across the Plasma Radius at High Density

- The higher density case results in ion root solutions across the entire plasma radius
 - Core ion root is caused by reduced T_e , $\nabla T_e \Rightarrow$ reduced electron flux
 - Without external drive the plasma would remain in the ion root
- Note that this threshold does not seem to require any additional fluxes (e.g. ECRH driven)



Ion Root is Predicted Across the Plasma Radius at High Density

- Measured E_r does not show large change with density
 - E_r measurements do not exclude core ion root solutions
- High density measurements closer to ion root solutions
- Planned experiment to operate at lower P/n to verify threshold behavior



Neoclassical Calculations Conserve Parallel Momentum

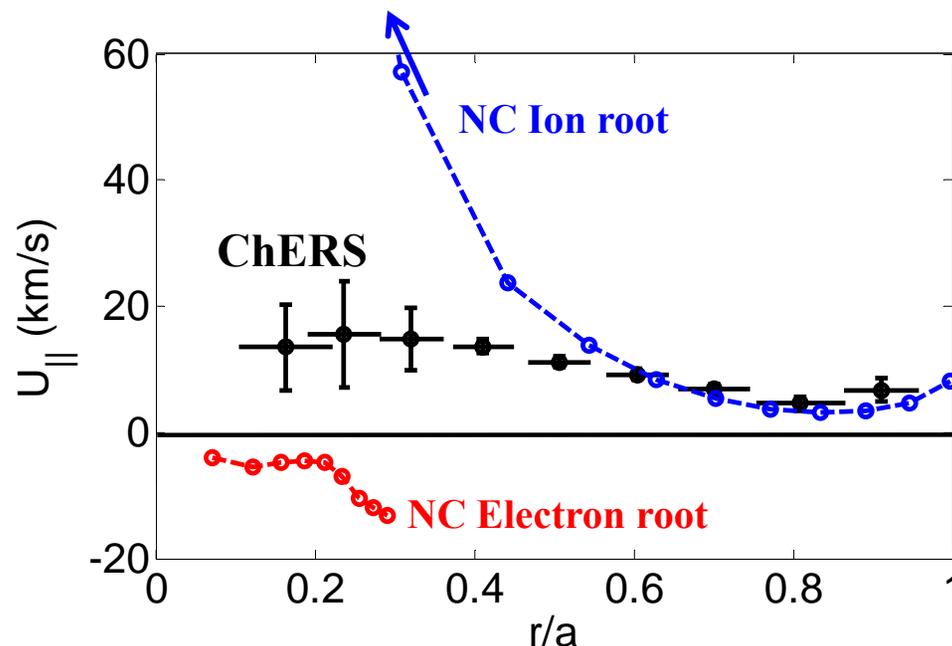
- Neoclassical calculations are performed using the PENTA¹ code
 - Based on the parallel momentum-conserving moments method of Sugama and Nishimura²
- Effects of parallel flow, interspecies collisions included
- Expressions used analytically reproduce intrinsic ambipolarity in symmetric limit
- In principle, this method can be applied to the full range of configurations:

tokamaks → rippled tokamaks → quasi-symmetric → conventional stellarators

Increasing effective ripple →

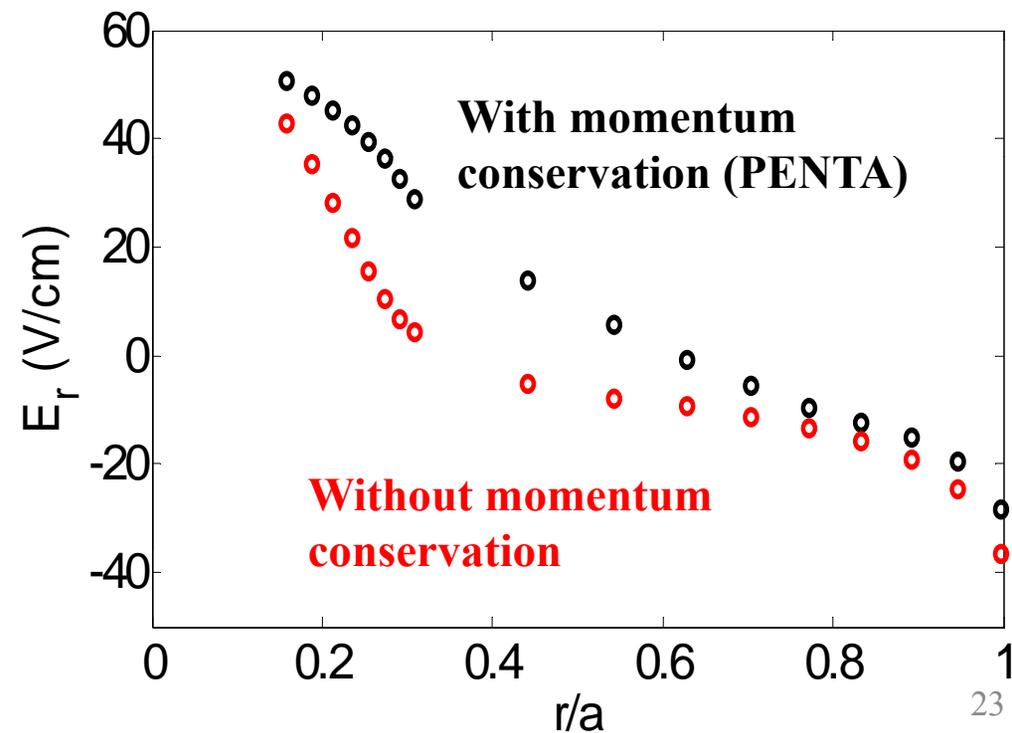
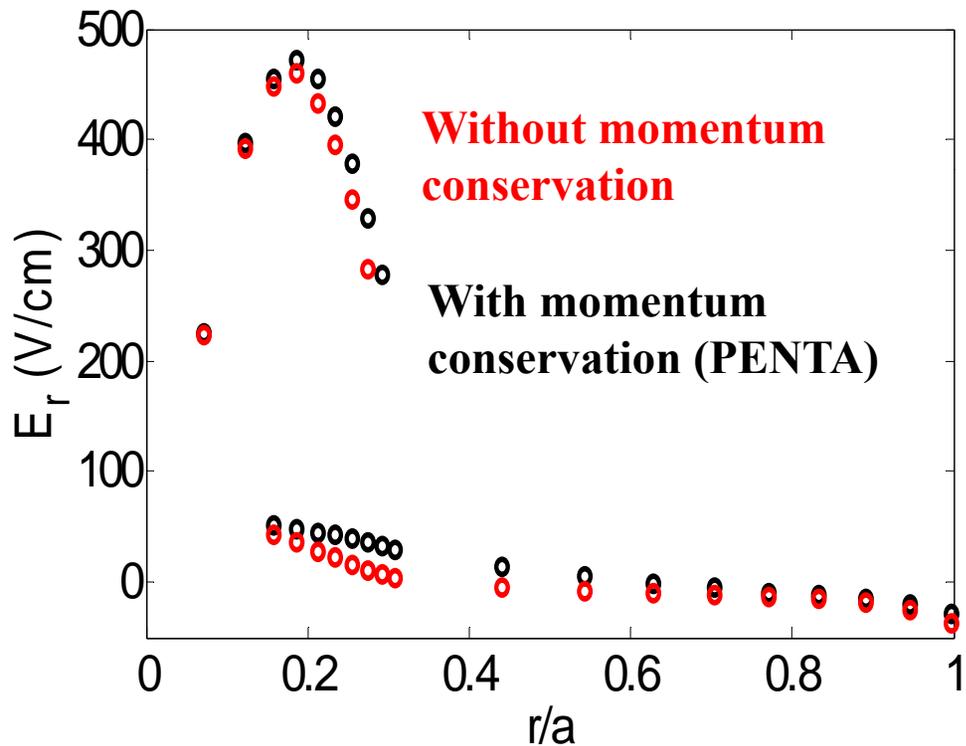
Momentum Conserving Calculations May be Important in Quasi-Symmetric Configurations

- Standard NC calculations assume $U_{\parallel} = 0$
 - Justified in conventional stellarators, because no $|B|$ symmetry leads to strong flow damping in all directions
 - Parallel flow may be large in quasi-symmetric configurations
- Large parallel flow (~ 10 - 25 km/s) measured in QHS
 - In agreement with PENTA predictions for $r/a > 0.6$
 - Very large ion root flows are inconsistent with assumption $U_i \ll v_{Ti}$



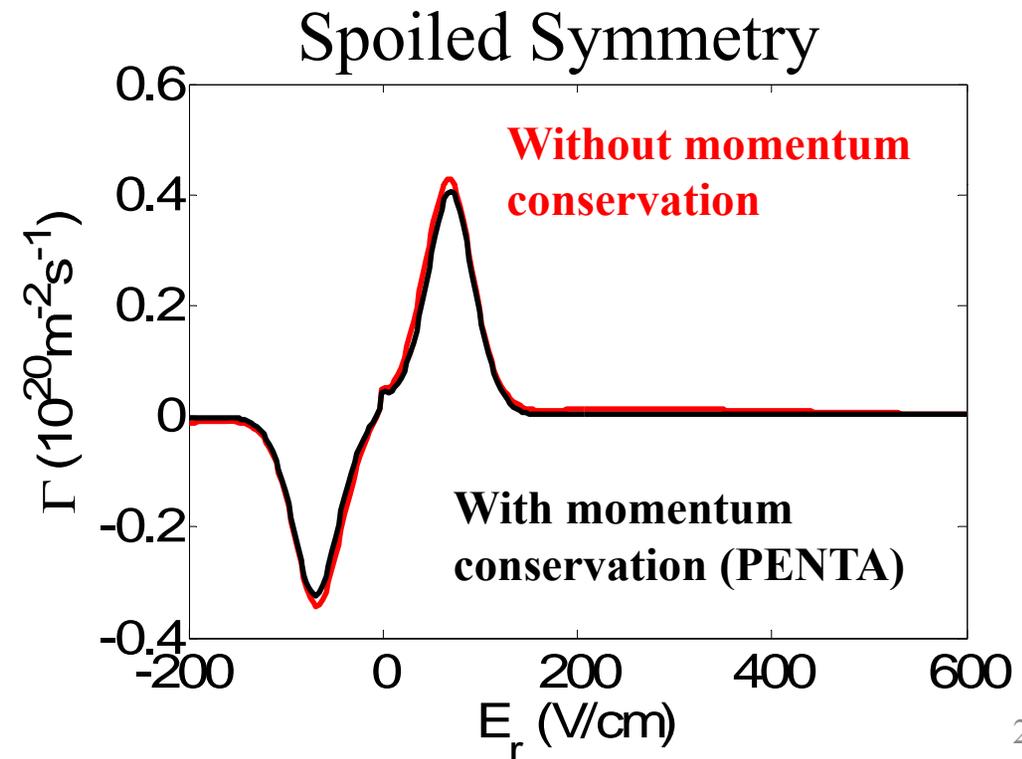
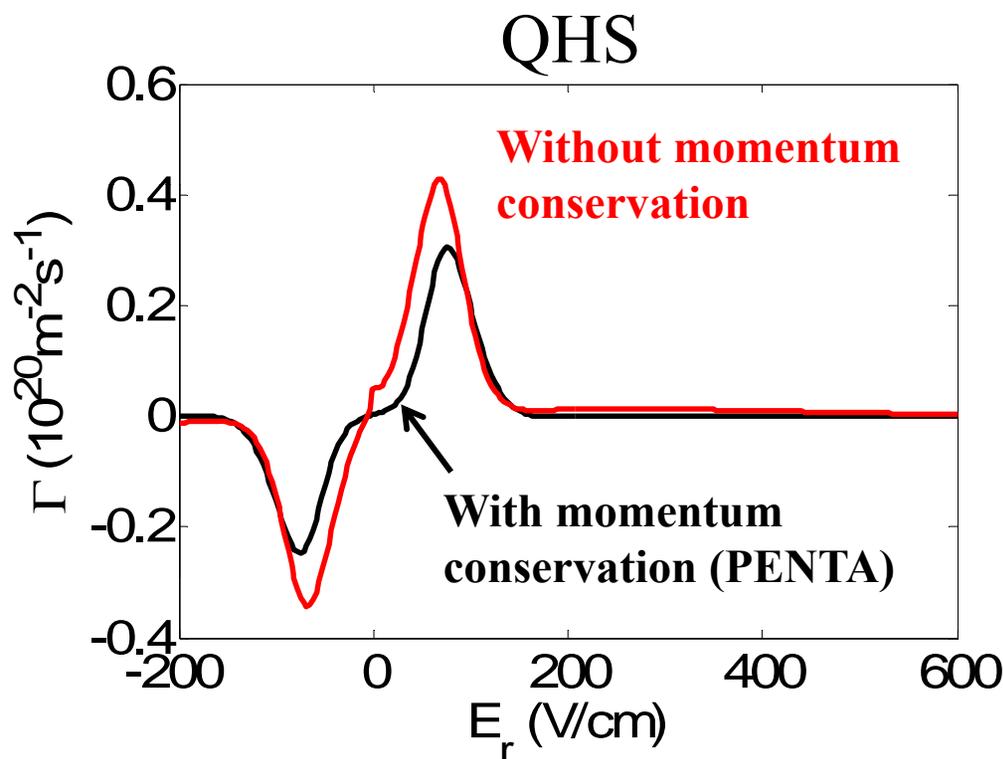
Momentum Conservation Modifies Neoclassical E_r

- Including momentum conservation changes ion root E_r by a factor of $\sim 2x$
- Effect is small in electron root, where ion flux is reduced due to poloidal resonance
- Modified E_r may be important for LMFP ion confinement
 - Change may be greater for larger T_i



Effect of Momentum Correction Decreases When Quasi-symmetry Spoiled

- Ion particle flux modified in QHS due to momentum conservation
 - Effect is masked due to resonance
- Change in ion flux due to flows is smaller when symmetry spoiled
- Detailed investigation of scaling with symmetry breaking in progress
 - Currently no flow, E_r measurements in spoiled symmetry configuration



Conclusions

- Neoclassically driven transport barrier in QHS
 - Peaked T_e profiles measured, electron root E_r with strong shear predicted
- 2D tokamak turbulent transport model well describes QHS anomalous transport
 - Core T_e profiles only reproduced when ExB shear included
- Density threshold for achieving CERC observed for fixed input power
 - Consistent with ion root neoclassical predictions
- Large parallel flow (10-25 km/s) measured in QHS
 - In agreement with predicted flow for $r/a > 0.6$
 - This flow and associated fluxes are accounted for in momentum conserving NC analysis (PENTA), neglected in “standard” stellarator NC calculations